

Name: RichardMATH 310  
R. HammackScore: 10**Directions:** Please answer in the space provided. No calculators. Please put all phones, etc., away.

1. Consider the basis
- $B = \{(1, 2), (3, 4)\}$
- of
- $\mathbb{R}^2$
- . Find the coordinate vector
- $[x]_B$
- for
- $x = (5, 6)$
- .

We know  $[x]_B = \begin{bmatrix} x \\ y \end{bmatrix}$  where  $x(1, 2) + y(3, 4) = (5, 6)$ .Thus  $(x + 3y, 2x + 4y) = (5, 6)$ .

This yields the system

$$\begin{cases} x + 3y = 5 \\ 2x + 4y = 6 \end{cases}$$

Solving,  $\left[ \begin{array}{cc|c} 1 & 3 & 5 \\ 2 & 4 & 6 \end{array} \right] \rightarrow \left[ \begin{array}{cc|c} 1 & 3 & 5 \\ 0 & -2 & -4 \end{array} \right]$

$$\rightarrow \left[ \begin{array}{cc|c} 1 & 3 & 5 \\ 0 & 1 & 2 \end{array} \right] \rightarrow \left[ \begin{array}{cc|c} 1 & 0 & -1 \\ 0 & 1 & 2 \end{array} \right] \quad \begin{array}{l} x = -1 \\ y = 2 \end{array}$$

Therefore  $\boxed{[x]_B = \begin{bmatrix} -1 \\ 2 \end{bmatrix}}$

Check  $-1(1, 2) + 2(3, 4) = (5, 6)$  ✓