

# **MATH 122**

(Day 7)

## **The Seventeen Tessellation Patterns**

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<http://www.people.vcu.edu/~rhammack/Math122/>

## KEY

Axis of reflection: 

Axis of glide reflection: 

Point of rotation: 

## Patterns Without Rotation Symmetry

## Patterns Without Rotation Symmetry



(p1)

## Patterns Without Rotation Symmetry



(p1) Reflections: NO  
Glide reflections: NO

## Patterns Without Rotation Symmetry



(p1) Reflections: NO  
Glide reflections: NO



(pm)

## Patterns Without Rotation Symmetry



(p1) Reflections: NO  
Glide reflections: NO



(pm) Reflections: YES

## Patterns Without Rotation Symmetry



(p1) Reflections: NO  
Glide reflections: NO



(pm) Reflections: YES  
Glide reflections: NO

## Patterns Without Rotation Symmetry



(p1) Reflections: NO  
Glide reflections: NO



(pm) Reflections: YES  
Glide reflections: NO



(pg)

## Patterns Without Rotation Symmetry



(p1) Reflections: NO  
Glide reflections: NO



(pm) Reflections: YES  
Glide reflections: NO



(pg) Reflections: NO

## Patterns Without Rotation Symmetry



(p1) Reflections: NO  
Glide reflections: NO



(pm) Reflections: YES  
Glide reflections: NO



(pg) Reflections: NO  
Glide reflections: YES

## Patterns Without Rotation Symmetry



(p1) Reflections: NO  
Glide reflections: NO



(pm) Reflections: YES  
Glide reflections: NO



(pg) Reflections: NO  
Glide reflections: YES



(cm)

## Patterns Without Rotation Symmetry



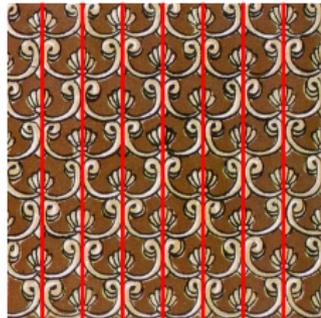
(p1) Reflections: NO  
Glide reflections: NO



(pm) Reflections: YES  
Glide reflections: NO



(pg) Reflections: NO  
Glide reflections: YES



(cm) Reflections: YES

## Patterns Without Rotation Symmetry



(p1) Reflections: NO  
Glide reflections: NO



(pm) Reflections: YES  
Glide reflections: NO



(pg) Reflections: NO  
Glide reflections: YES



(cm) Reflections: YES  
Glide reflections: YES

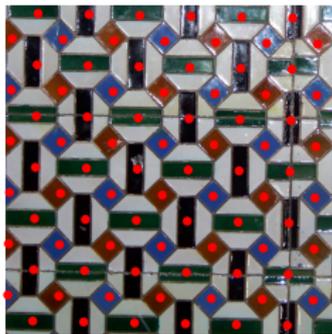
## Patterns with Rotation by $180^\circ$

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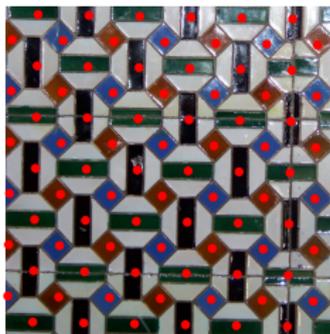
(p2)

## Patterns with Rotation by $180^\circ$



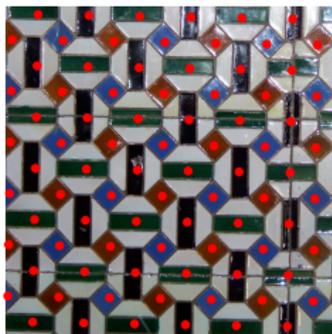
(p2)

## Patterns with Rotation by $180^\circ$

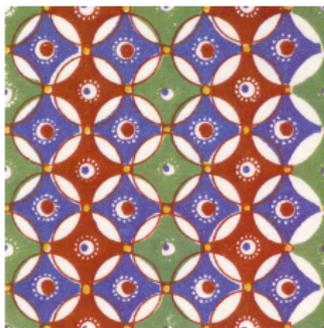


(p2) Reflection: NO  
Glide reflection: NO

## Patterns with Rotation by $180^\circ$

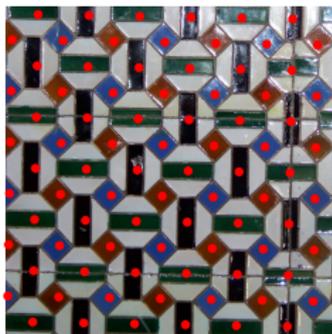


(p2) Reflection: NO  
Glide reflection: NO

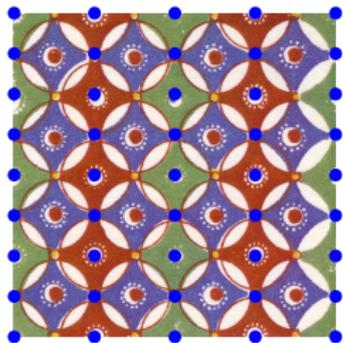


(pmm)

## Patterns with Rotation by $180^\circ$

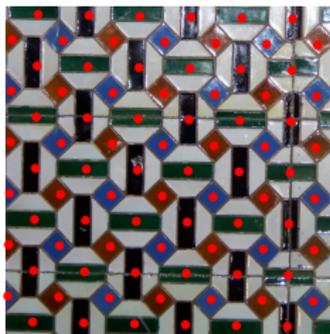


(p2) Reflection: NO  
Glide reflection: NO

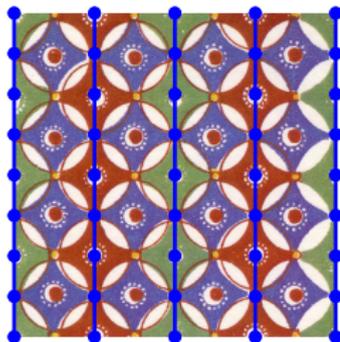


(pmm)

## Patterns with Rotation by $180^\circ$

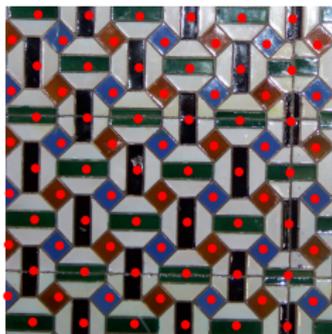


(p2) Reflection: NO  
Glide reflection: NO

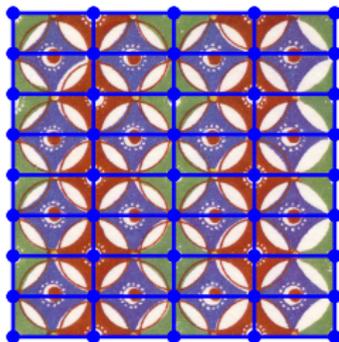


(pmm) Reflection: YES

## Patterns with Rotation by $180^\circ$

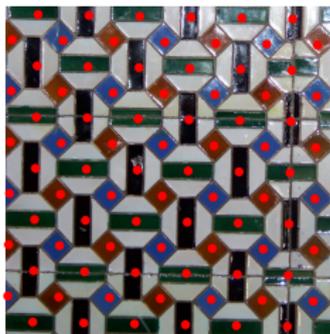


(p2) Reflection: NO  
Glide reflection: NO

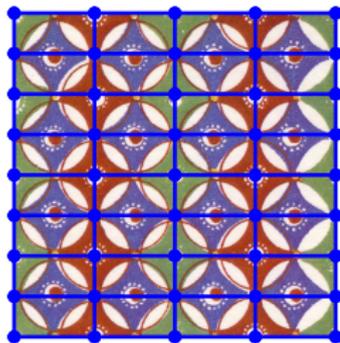


(pmm) Reflection: YES

## Patterns with Rotation by $180^\circ$

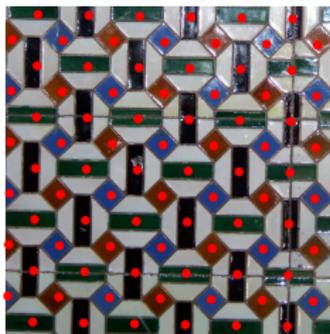


(p2) Reflection: NO  
Glide reflection: NO

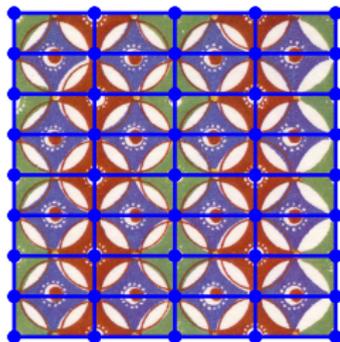


(pmm) Reflection: YES  
Glide reflection: NO

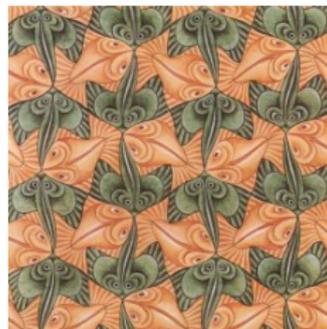
## Patterns with Rotation by $180^\circ$



(p2) Reflection: NO  
Glide reflection: NO

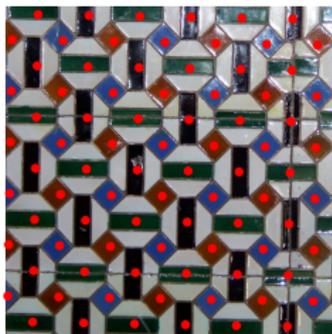


(pmm) Reflection: YES  
Glide reflection: NO

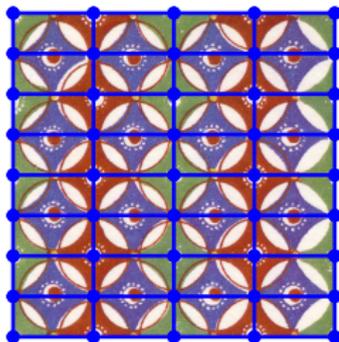


(pgg)

## Patterns with Rotation by $180^\circ$



(p2) Reflection: NO  
Glide reflection: NO

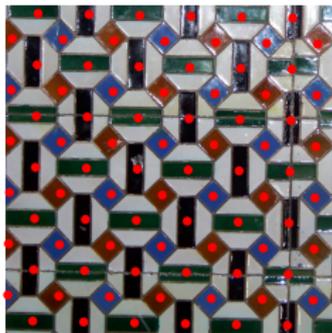


(pmm) Reflection: YES  
Glide reflection: NO

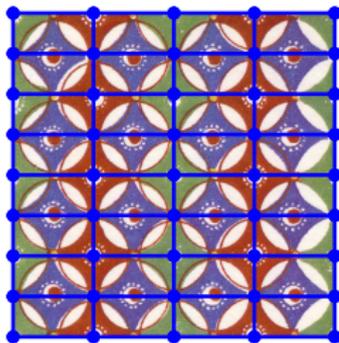


(pgg)

## Patterns with Rotation by $180^\circ$



(p2) Reflection: NO  
Glide reflection: NO

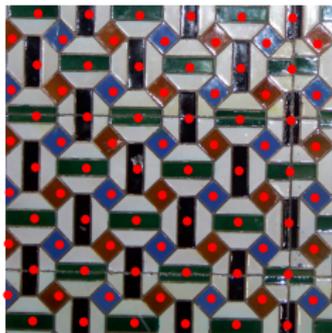


(pmm) Reflection: YES  
Glide reflection: NO

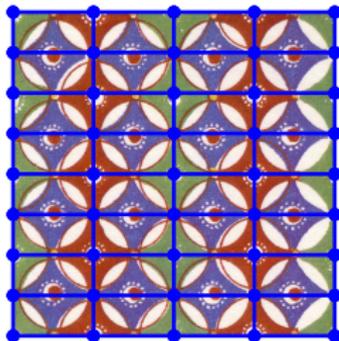


(pgg) Reflection: NO

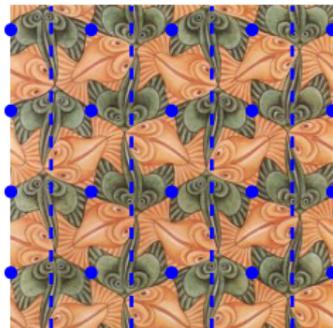
## Patterns with Rotation by $180^\circ$



(p2) Reflection: NO  
Glide reflection: NO

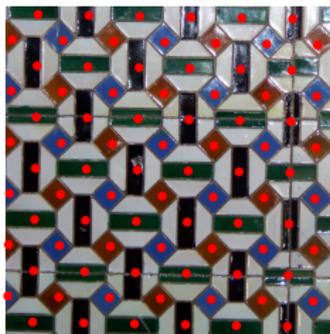


(pmm) Reflection: YES  
Glide reflection: NO

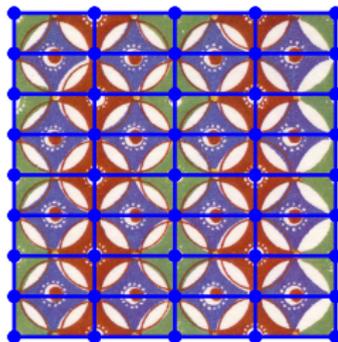


(pgg) Reflection: NO  
Glide reflection: YES

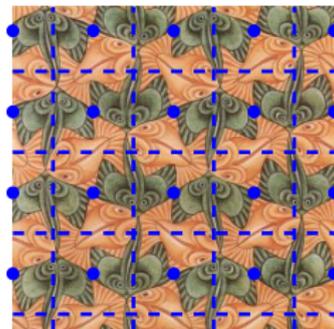
## Patterns with Rotation by $180^\circ$



(p2) Reflection: NO  
Glide reflection: NO

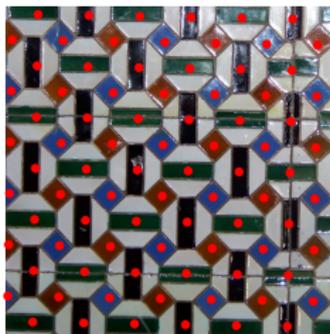


(pmm) Reflection: YES  
Glide reflection: NO

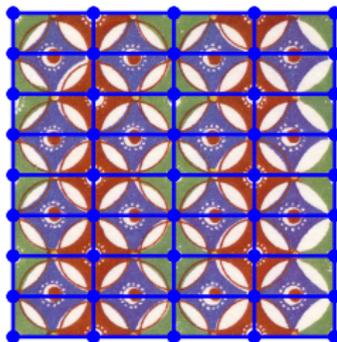


(pgg) Reflection: NO  
Glide reflection: YES

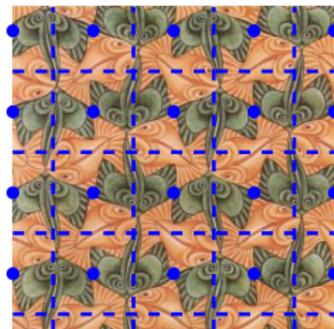
## Patterns with Rotation by $180^\circ$



(p2) Reflection: NO  
Glide reflection: NO



(pmm) Reflection: YES  
Glide reflection: NO

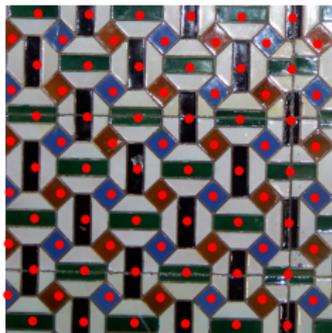


(pgg) Reflection: NO  
Glide reflection: YES

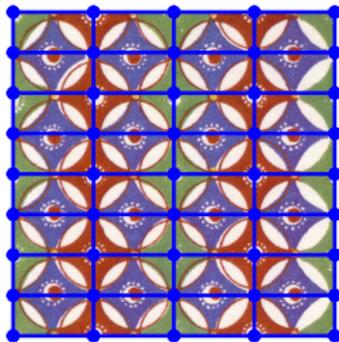


(cmm)

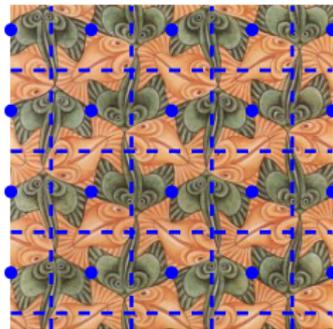
## Patterns with Rotation by $180^\circ$



(p2) Reflection: NO  
Glide reflection: NO



(pmm) Reflection: YES  
Glide reflection: NO

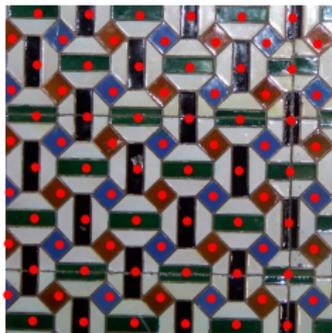


(pgg) Reflection: NO  
Glide reflection: YES

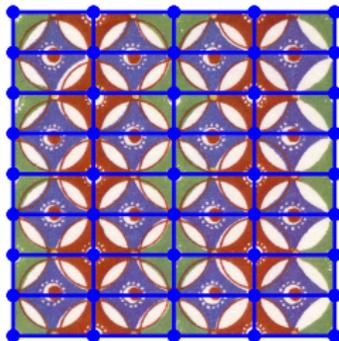


(cmm)

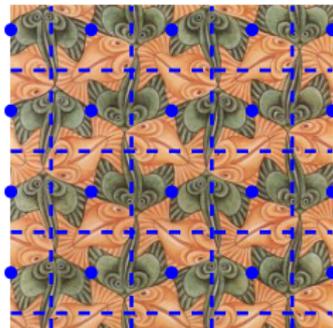
## Patterns with Rotation by $180^\circ$



(p2) Reflection: NO  
Glide reflection: NO



(pmm) Reflection: YES  
Glide reflection: NO

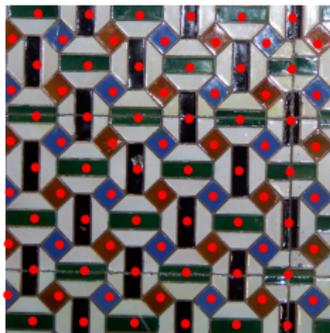


(pgg) Reflection: NO  
Glide reflection: YES

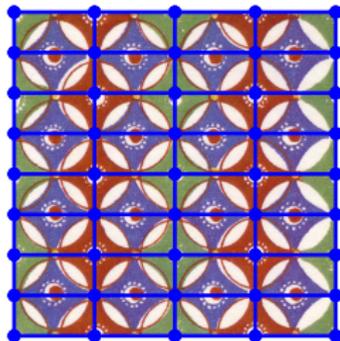


(cmm) Reflection: YES

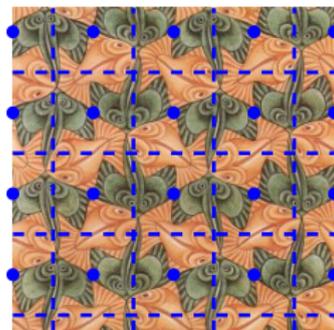
## Patterns with Rotation by $180^\circ$



(p2) Reflection: NO  
Glide reflection: NO



(pmm) Reflection: YES  
Glide reflection: NO

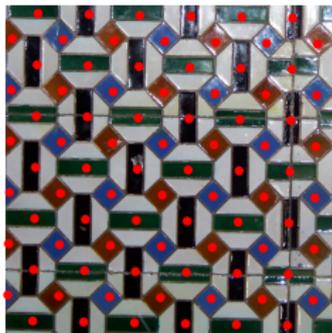


(pgg) Reflection: NO  
Glide reflection: YES

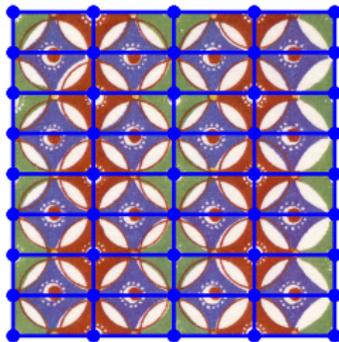


(cmm) Reflection: YES

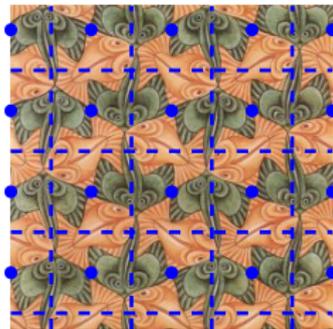
## Patterns with Rotation by $180^\circ$



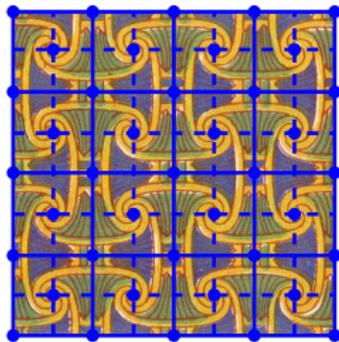
(p2) Reflection: NO  
Glide reflection: NO



(pmm) Reflection: YES  
Glide reflection: NO

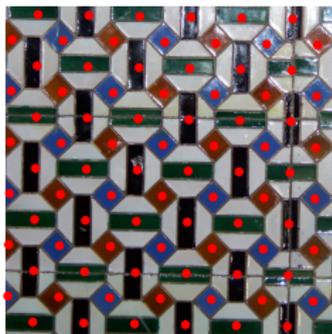


(pgg) Reflection: NO  
Glide reflection: YES

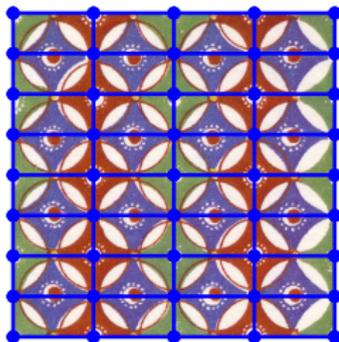


(cmm) Reflection: YES  
Glide reflection: YES

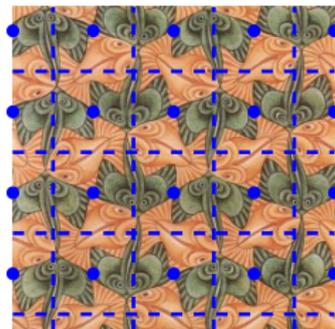
## Patterns with Rotation by $180^\circ$



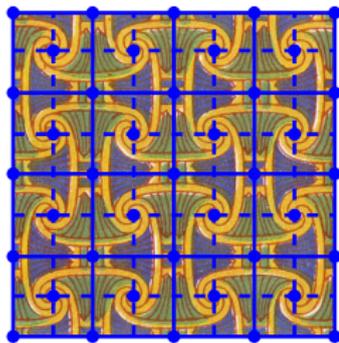
(p2) Reflection: NO  
Glide reflection: NO



(pmm) Reflection: YES  
Glide reflection: NO



(pgg) Reflection: NO  
Glide reflection: YES

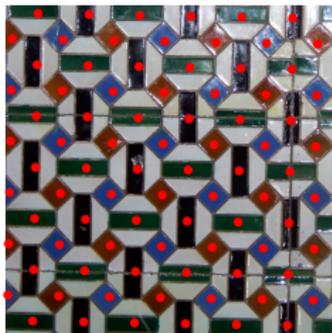


(cmm) Reflection: YES  
Glide reflection: YES

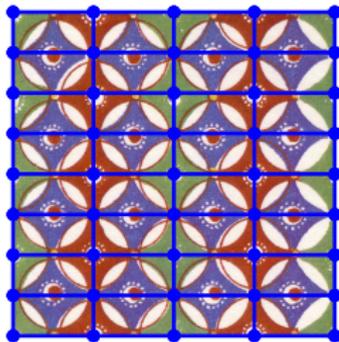


(pmg)

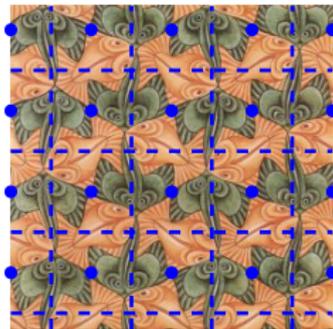
## Patterns with Rotation by $180^\circ$



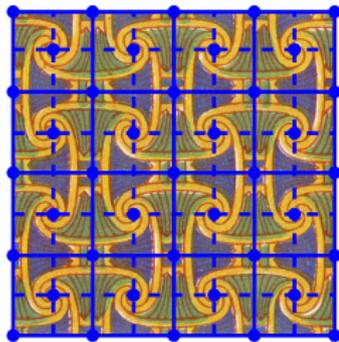
(p2) Reflection: NO  
Glide reflection: NO



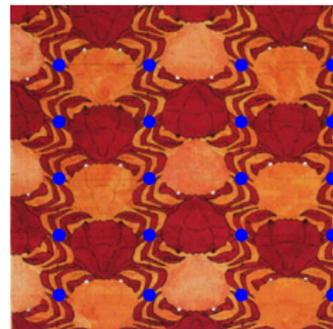
(pmm) Reflection: YES  
Glide reflection: NO



(pgg) Reflection: NO  
Glide reflection: YES

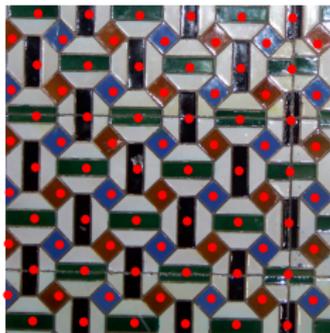


(cmm) Reflection: YES  
Glide reflection: YES

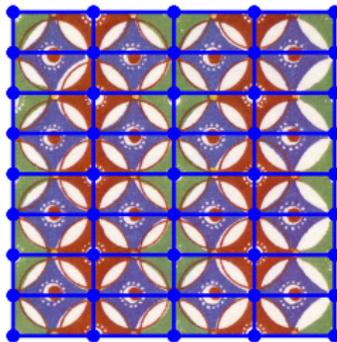


(pmg)

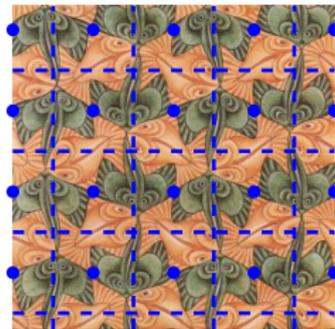
## Patterns with Rotation by $180^\circ$



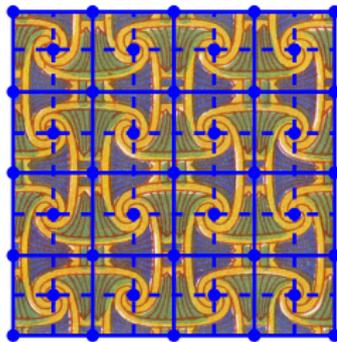
(p2) Reflection: NO  
Glide reflection: NO



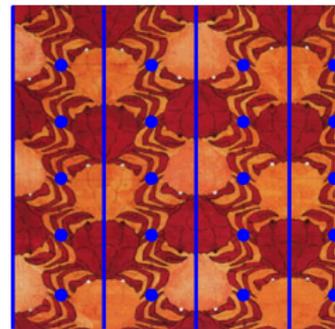
(pmm) Reflection: YES  
Glide reflection: NO



(pgg) Reflection: NO  
Glide reflection: YES

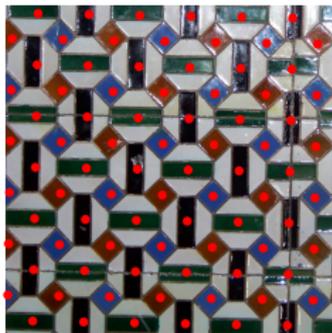


(cmm) Reflection: YES  
Glide reflection: YES

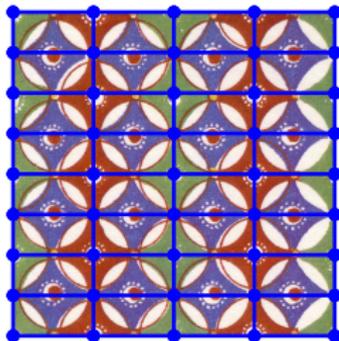


(pmg) Reflection: YES

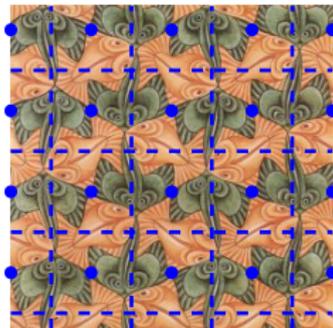
## Patterns with Rotation by $180^\circ$



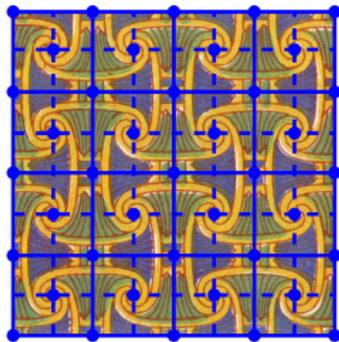
(p2) Reflection: NO  
Glide reflection: NO



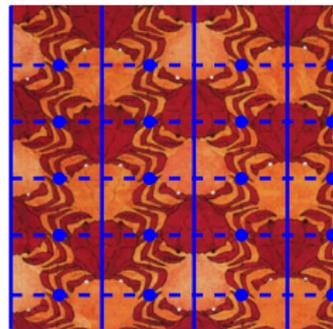
(pmm) Reflection: YES  
Glide reflection: NO



(pgg) Reflection: NO  
Glide reflection: YES



(cmm) Reflection: YES  
Glide reflection: YES



(pmg) Reflection: YES  
Glide reflection: YES

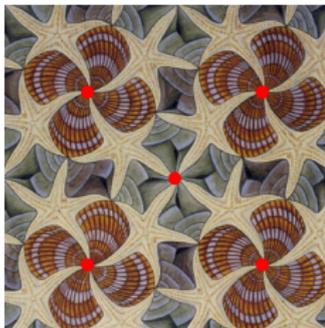
Patterns with Rotation by  $90^\circ$

## Patterns with Rotation by $90^\circ$



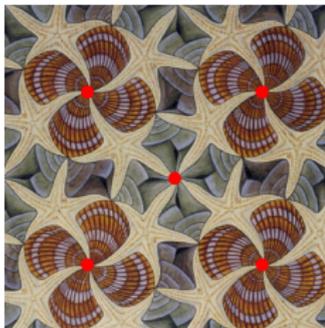
(p4)

## Patterns with Rotation by $90^\circ$



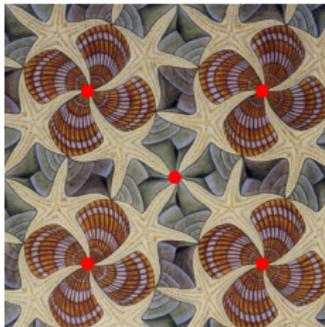
(p4)

## Patterns with Rotation by $90^\circ$

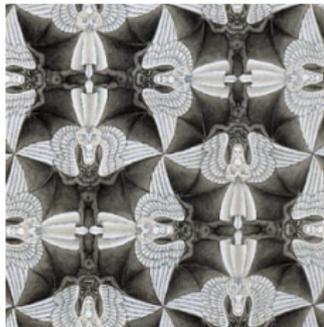


(p4) Reflections: NO  
Glide reflections: NO

## Patterns with Rotation by $90^\circ$

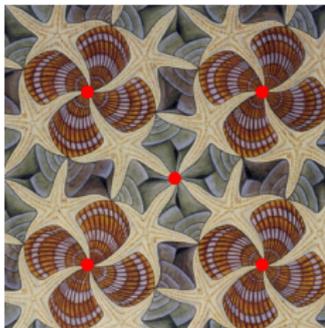


(p4) Reflections: NO  
Glide reflections: NO

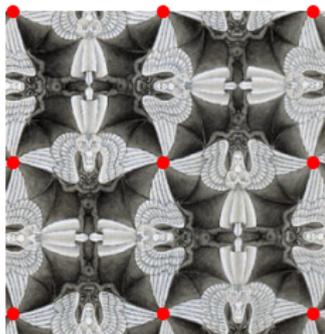


(p4g)

## Patterns with Rotation by $90^\circ$

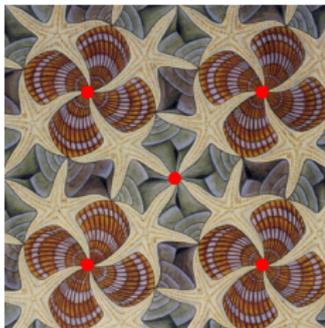


(p4) Reflections: NO  
Glide reflections: NO

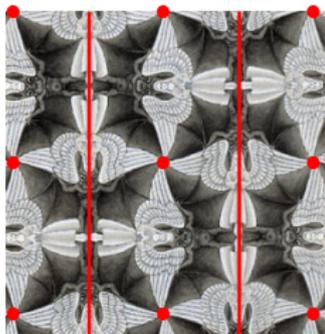


(p4g)

## Patterns with Rotation by $90^\circ$

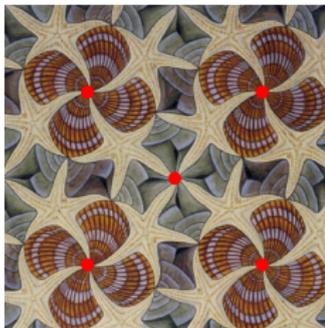


(p4) Reflections: NO  
Glide reflections: NO

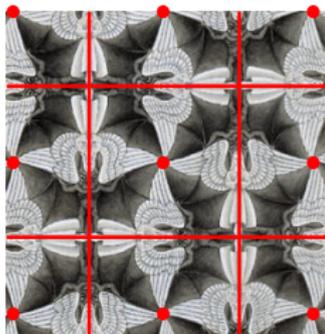


(p4g) Reflections: YES

## Patterns with Rotation by $90^\circ$

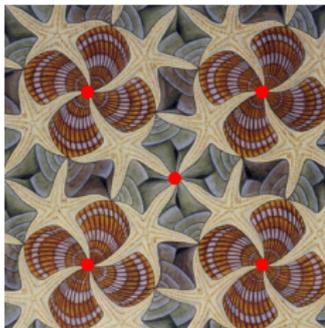


(p4) Reflections: NO  
Glide reflections: NO

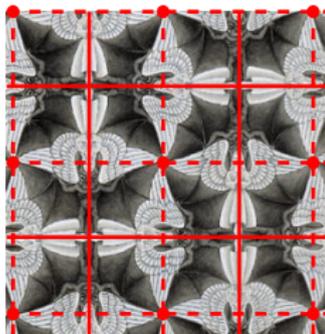


(p4g) Reflections: YES

## Patterns with Rotation by $90^\circ$

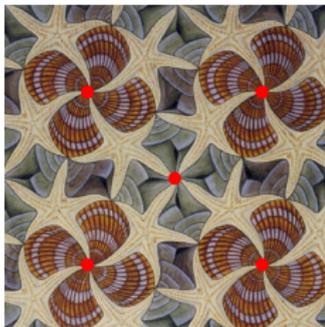


(p4) Reflections: NO  
Glide reflections: NO

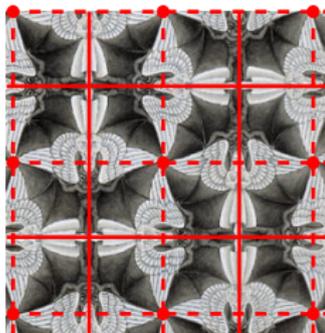


(p4g) Reflections: YES  
Glide reflections: YES

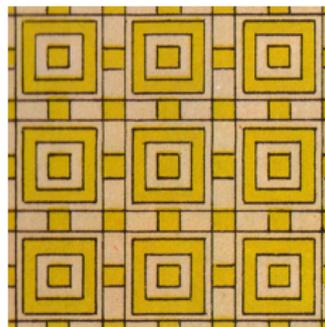
## Patterns with Rotation by $90^\circ$



(p4) Reflections: NO  
Glide reflections: NO

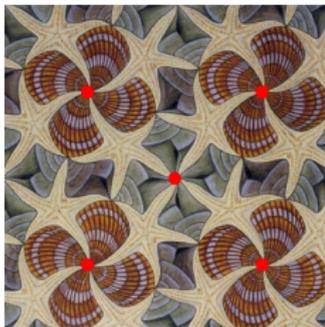


(p4g) Reflections: YES  
Glide reflections: YES

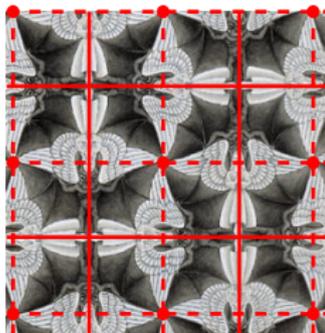


(p4m) Reflections: YES  
Glide reflections: YES

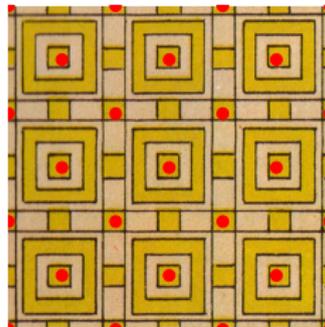
## Patterns with Rotation by $90^\circ$



(p4) Reflections: NO  
Glide reflections: NO

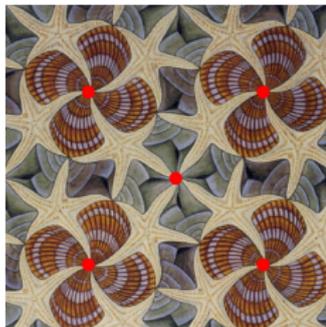


(p4g) Reflections: YES  
Glide reflections: YES

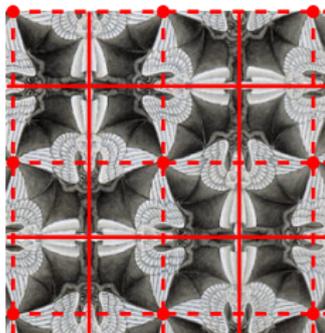


(p4m) Reflections: YES  
Glide reflections: YES

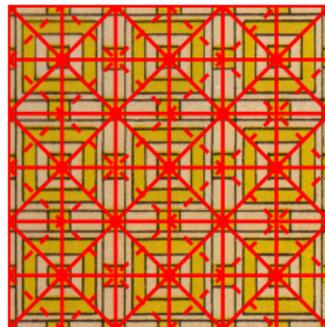
## Patterns with Rotation by $90^\circ$



(p4) Reflections: NO  
Glide reflections: NO



(p4g) Reflections: YES  
Glide reflections: YES



(p4m) Reflections: YES  
Glide reflections: YES

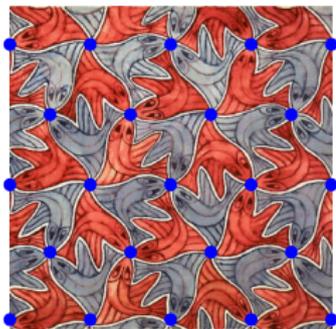
Patterns with Rotation by  $120^\circ$

## Patterns with Rotation by $120^\circ$



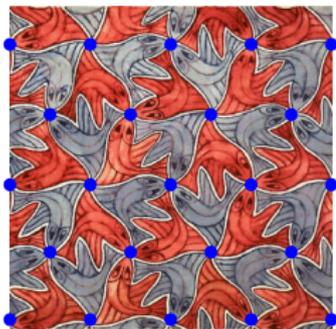
(p3)

## Patterns with Rotation by $120^\circ$



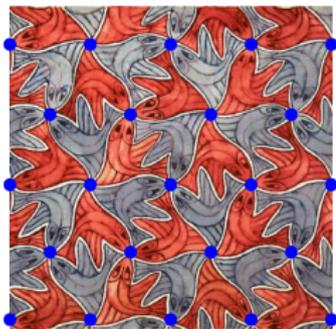
(p3)

## Patterns with Rotation by $120^\circ$



(p3) Reflections: NO  
Glide reflections: NO

## Patterns with Rotation by $120^\circ$

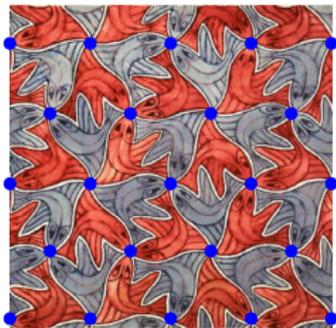


(p3) Reflections: NO  
Glide reflections: NO

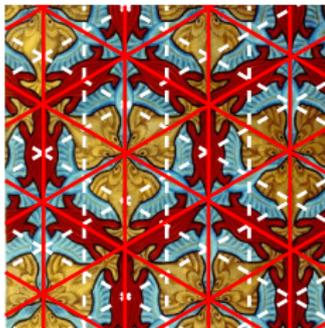


(p3m1)

## Patterns with Rotation by $120^\circ$

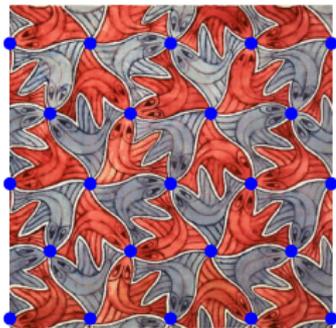


(p3) Reflections: NO  
Glide reflections: NO

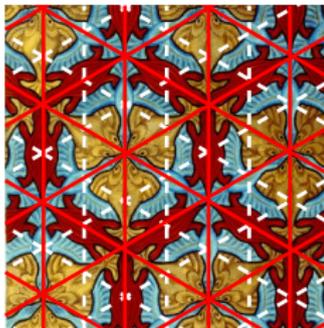


(p3m1) Reflections: YES  
Glide reflections: YES

## Patterns with Rotation by $120^\circ$



(p3) Reflections: NO  
Glide reflections: NO

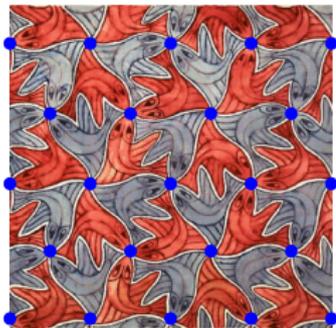


(p3m1) Reflections: YES  
Glide reflections: YES

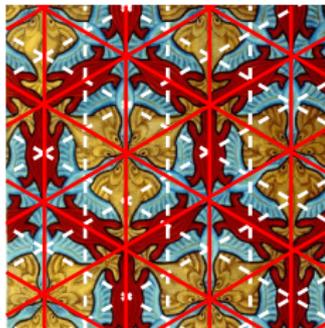


(p31m)

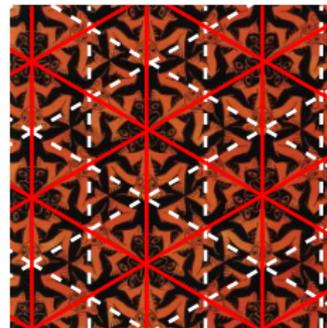
## Patterns with Rotation by $120^\circ$



(p3) Reflections: NO  
Glide reflections: NO



(p3m1) Reflections: YES  
Glide reflections: YES



(p31m) Reflections: YES  
Glide reflections: YES

## Patterns with Rotation by $60^\circ$



(p6)

## Patterns with Rotation by $60^\circ$



(p6)

## Patterns with Rotation by $60^\circ$

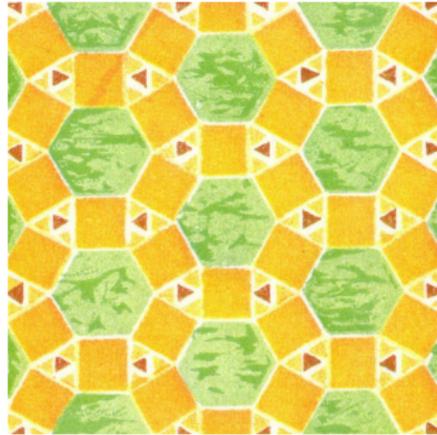


(p6) Reflection: NO  
Glide reflection: NO

## Patterns with Rotation by $60^\circ$



(p6) Reflection: NO  
Glide reflection: NO

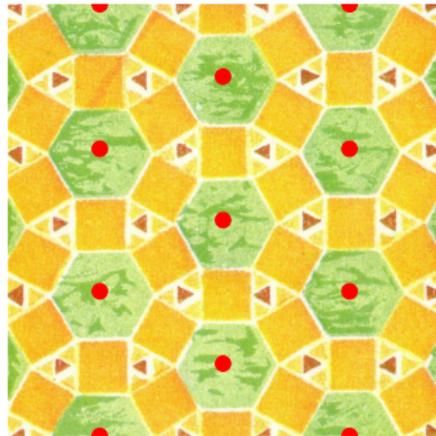


(p6m) Reflection: YES  
Glide reflection: YES

## Patterns with Rotation by $60^\circ$



(p6) Reflection: NO  
Glide reflection: NO

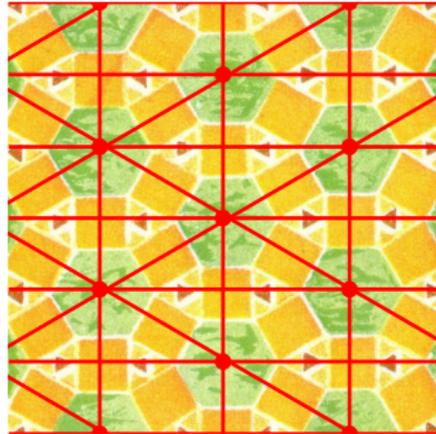


(p6m) Reflection: YES  
Glide reflection: YES

## Patterns with Rotation by $60^\circ$



(p6) Reflection: NO  
Glide reflection: NO

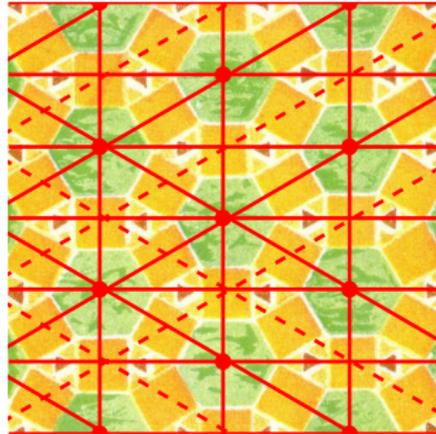


(p6m) Reflection: YES  
Glide reflection: YES

## Patterns with Rotation by $60^\circ$

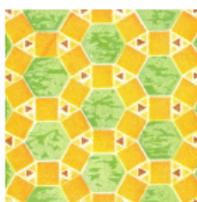
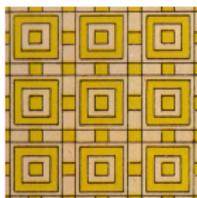
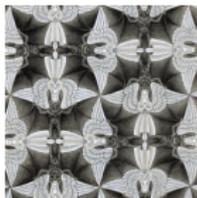
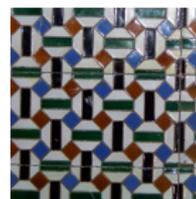


(p6) Reflection: NO  
Glide reflection: NO



(p6m) Reflection: YES  
Glide reflection: YES

# The 17 Tessellation Symmetry Types



[www.people.vcu.edu/~rhammack/Math122/](http://www.people.vcu.edu/~rhammack/Math122/)